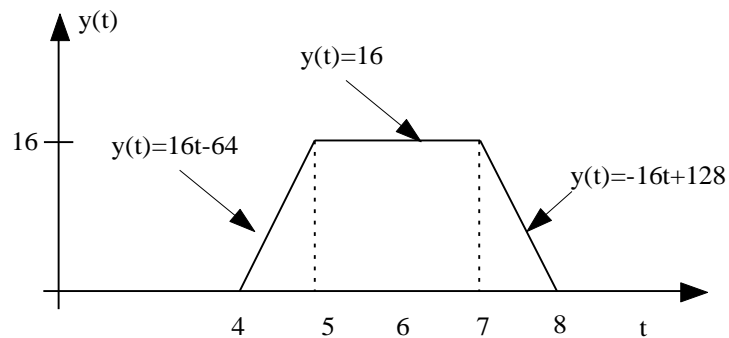


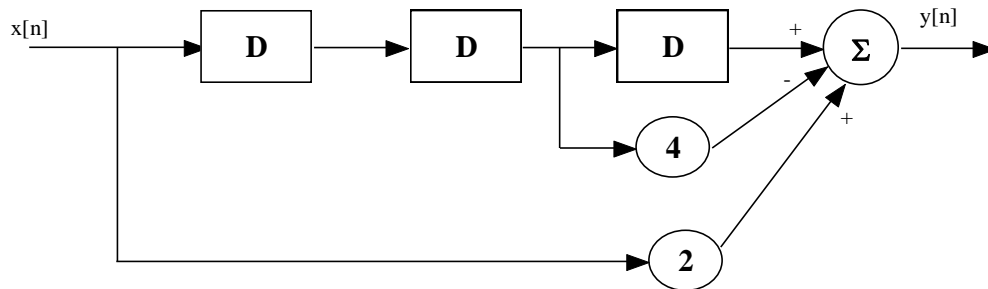
Q1)

[4]



Q2:-

a)



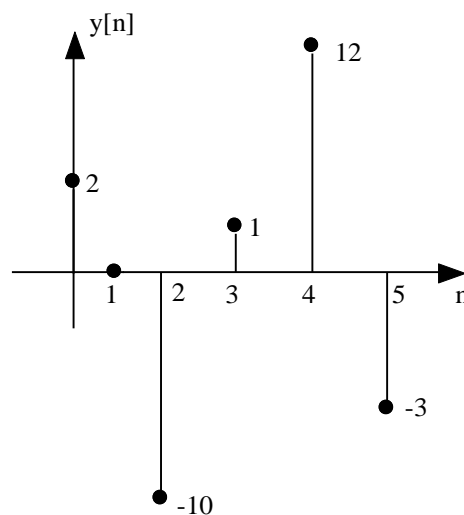
[5]

b)

$$h[n] = 2\delta[n] - 4\delta[n-2] + \delta[n-3]$$

c)

$$y[n] = x[n] * h[n] = \{1, 0, -3\} * \{2, 0, -4, 1\} = \{2, 0, -10, 1, 12, -3\}$$



**Q3 -**

[4]

a)  $3\delta(t - 5) \Leftrightarrow 3e^{-5s}$  ROC: all  $s$  except  $s = -\infty$

b)  $2u(t - 3) \Leftrightarrow \frac{2e^{-3s}}{s}$  ROC:  $\text{Re}(s) > 0$

c)  $x(t) = 2tu(t + 2) \Leftrightarrow 2 \left[ \frac{e^{2s}}{s^2} - \frac{2e^{2s}}{s} \right]$  ROC:  $\text{Re}(s) > 0$

d)

$$x(t) = e^{-t}u(t) - e^{-t}u(t - 2) = e^{-t}u(t) - e^{-2}e^{-(t-2)}u(t - 2)$$

$$X(s) = \frac{1}{s+1} - e^{-2}e^{-2s} \frac{1}{s+1} = \frac{1}{s+2} (1 - e^{-2(s+1)}) \quad \text{ROC: } \text{Re}(s) > -2$$

**Q4 -**

[7]

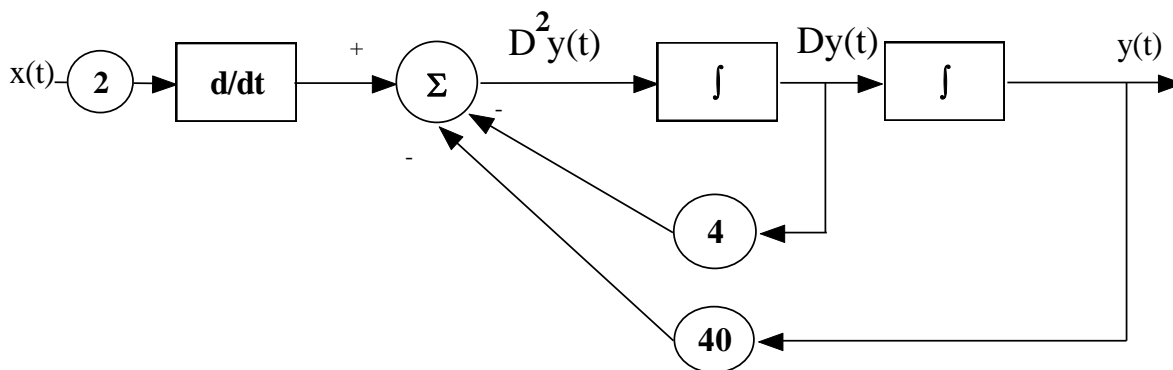
a)

$$x(t) = \frac{1}{2} \frac{dy}{dt} + 2y(t) + 20 \int y(\tau) d\tau$$

$$\frac{1}{2} D^2 y(t) + 2Dy(t) + 20y(t) = Dx(t)$$

$$D^2 y(t) = 2Dx(t) - 4Dy(t) - 40y(t)$$

b)



c)

$$D^2 y(t) + 4Dy(t) + 40y(t) = 2Dx(t)$$

The impulse response of the function

$$D^2 y(t) + 4Dy(t) + 40y(t) = x(t)$$

Can be found using

$$D^2 \hat{h}(t) + 4D \hat{h}(t) + 40 \hat{h}(t) = \delta(t)$$

The homogeneous solution is given as  $\hat{h}(t) = c_1 e^{(-2+6j)t} + c_2 e^{(-2-6j)t}$

With  $\hat{h}(0) = 0$  and  $\hat{h}^{(1)}(0) = 1$

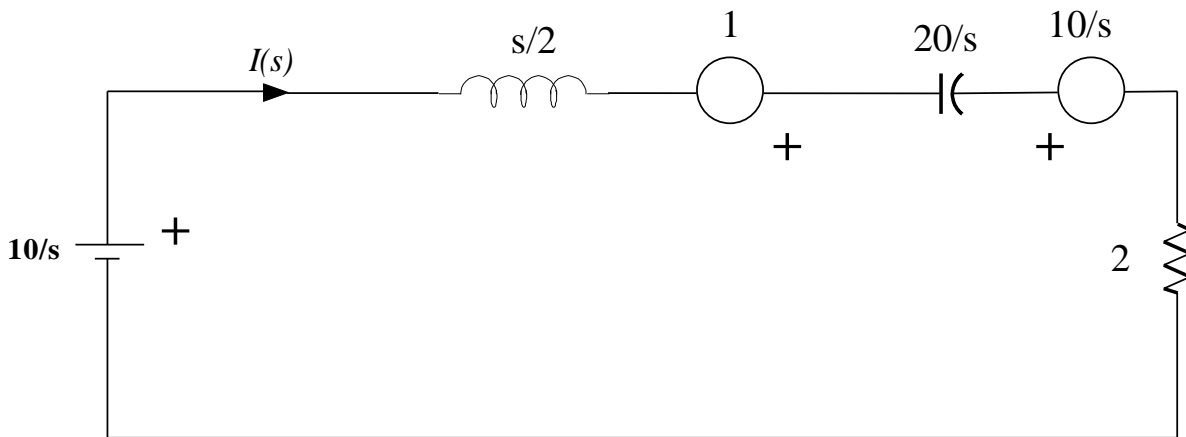
Thus

$$\hat{h}(t) = \frac{-j}{12} e^{(-2+6j)t} + \frac{j}{12} e^{(-2-6j)t}$$

The required impulse response given as  $h(t) = 2D \hat{h}(t) = \left[ \frac{(6+2j)}{6} e^{(-2+6j)t} + \frac{(6-2j)}{6} e^{(-2-6j)t} \right] u(t)$

d)

$$i(0^-)=2, v_c(0^-)=10$$



$$\frac{1}{2} s I(s) - 1 + 2 I(s) + \frac{20}{s} I(s) + \frac{10}{s} = \frac{10}{s}$$

$$I(s) = \frac{2s}{s^2 + 4s + 40} = 2 \frac{s+2}{(s+2)^2 + 6^2} - \frac{2}{3} \frac{6}{(s+2)^2 + 6^2}$$

$$i(t) = e^{-2t} \left( 2 \cos 6t - \frac{2}{3} \sin 6t \right) u(t)$$